



Decomposition of 3D medical image based on Fast and Adaptive Bidimensional Empirical Mode Decomposition

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ABSTRACT

Three-dimensional (3D) imaging and display have been subjects of much research due to their diverse benefits and applications. This paper presents a new approach for decomposing the three-dimensional medical images using Bidimensional Empirical Mode Decomposition (BEMD). The BEMD is an extension of the Empirical Mode Decomposition (EMD), which can decompose non-linear and non-stationary signals into basis functions called the Intrinsic Mode Functions (IMFs). IMFs are monocomponent functions that have well defined instantaneous frequencies. This decomposition, obtained by a process known as sifting process, allows extracting the structures at different scales and spatial frequencies with modulation in amplitudes and frequency. BEMD decomposes an image into bidimensional BIMFs. This paper suggests a simple, but effective, method for decomposing a three-dimensional medical image into basis function. This approach is neither parametric nor data driven, which means it does not depend on a priori basis set. Moreover, it preserves the totality of information in term of the quality of the reconstructed 3D image. The performance of this approach, using the BEMD, is approved with some medical images.

Keywords: *Bidimensional Empirical Mode Decomposition (BEMD), Fast and Adaptive BEMD (FABEMD), Intrinsic Mode Function (IMF), 3D Reconstruction.*

1 INTRODUCTION

The volume of medical images produced in the world is constantly increasing. Millions of three-dimensional medical images (3D) are produced each year to diagnose or monitor a therapeutic effect. They provide data on the form and functioning of body organs. Unfortunately, these data are extremely difficult to exploit in a quantitative and objective manner [1].

The applications of three-dimensional reconstruction are numerous and varied: they extend from medicine [2], geography to the shipbuilding. In medicine, generally in the biomedical, reconstruction addresses the areas: anatomy [3, 4], electron microscopy and confocal [5], radiology [6], of surgery, cell biology, etc...

3D reconstruction is particularly popular in

microscopy. Indeed, the microscope lets to see very small structures but unfortunately provides only flat image. However, tissues, cells or subcellular structures have a three-dimensional architecture that the microscope cannot make it. The biologist is thus deprived of certain information. The scanning electron microscope overcomes this problem but it lacks flexibility and is limited in some cases (impossibility of seeing through the objects). In this case it is the 3D reconstruction takes over.

Three-dimensional reconstruction is also used in:

- Computer Aided Design: automotive, shipbuilding.
- Architecture and building technology: construction aid, study of the structure of materials (searching for cracks, grains, bubbles ...).

- Geography: mapping (building of models from sections taken at different altitudes).

In medicine, three-dimensional reconstruction from serial sections is not a recent problem that dealt with new forms 3D acquisition modality. Some good manual 3D reconstruction techniques back to centuries before. They yield two different modes of reconstruction: graphic and rigid [7, 8]. Until now, several methods have been proposed to reconstruct a 3D model from structured data in 2D slices. The Marching Cubes algorithm proposed by W.E. Lorensen and H.E. Cline [9] and the algorithm based on the Delaunay triangulation proposed by J.D. Boissonnat and B. GEIGER [10] are references in this area.

Among the methods of image decomposition existing in the literature (for example wavelet [11]), Empirical Mode Decomposition (EMD) [12] is a flexible technique of signal decomposition. EMD considers the signal to be processed on the scale of its local oscillations. The basic idea is to decompose a signal into a sum of components, called empirical mode or Intrinsic Mode Functions (IMFs). Each of IMF is a zero mean waveform, modulated in amplitude and frequency. It has a self-adaptive nature that enables it to identify changes in the signal, whether in terms of amplitude or frequency. Decomposition is not based on a predefined criterion, unlike the wavelet decomposition which requires a mother wavelet or kernel. Many researches proved that it is a very powerful tool for adaptive multi-scale analysis of non-stationary and non-linear signals, and took a place among the best known decomposition filters. The EMD is successfully applied in many fields ranging from pure scientific context to engineering [13, 14, 15, 16, 17, 18, 19, 20, 21].

This decomposition technique has also been extended to new ones that analyze bidimensional images. They are known by Bidimensional EMD (BEMD), image EMD (IEMD), 2D EMD etc [22, 23]. Interpolation is an important issue both in the field of image signal for the estimation and the extraction of the IMFs from extrema. Different procedures can be used to calculate average envelope [12]. In FABEMD (Fast and Adaptive BEMD), order statistics filters are employed to estimate the envelope surfaces from the data instead of surface interpolation.

In this paper, we propose an extension of BEMD for three-dimensional medical images based on 3D reconstruction. The 3D decomposition schemes process the data as multi 2D slices with BEMD like

technique. The main conceptual innovations are the introduction of Intrinsic Mode Functions based on global properties of the 3D medical image which makes the image sequence into a set of modes.

2 BIDIMENSIONAL EMPIRICAL MODE DECOMPOSITION

EMD is an adaptive decomposition of signals [24], introduced by Huang [12] for one-dimensional data and then extended to Bidimensional signals.

The novel BEMD approach is a highly adaptive decomposition [25]. It is based on the characterization of the image with this decomposition in Intrinsic Mode Function (IMF) where the image can be decomposed into a redundant set of composite images called IMFs and a residue. An IMF is characterized by two specific properties [26]:

- The number of zero crossing and the number of extrema points is equal or differs only by one.
- It has a zero local mean.

The algorithm is described as follows:

Given an image I

1. Fixed. ε , $i = 1, r_{i-1} = I$ (residue)
2. Extraction of the i^{th} IMF:
 - a. Initialization: $h_{i,j-1} = r_{i-1}, j = 1$
 - b. Extract local minima and maxima of $h_{i,j-1}$
 - c. Interpolate the local extrema to construct the upper and the lower envelope respectively, $U_{i,j-1}$ and $L_{i,j-1}$
 - d. Calculate the average of the two envelopes:

$$m_{i,j-1} = \frac{U_{i,j-1} + L_{i,j-1}}{2}$$

- e. Update:

$$h_{i,j} = h_{i,j-1} - m_{i,j-1}, j = j + 1$$

- f. Calculate the stopping criterion :(Standard Deviation)

$$SD = \sum_{x=1}^M \sum_{y=1}^N \frac{|h_{i,j}(x,y) - h_{i,j-1}(x,y)|^2}{|h_{i,j-1}(x,y)|^2}$$

- g. Decision: Repeat steps (b) to (f) until $SD(j) \leq \varepsilon$, and then put

$$IMF_i = h_{i,j}(i^{eme} IMF)$$

3. Update residual:

$$r_i = r_{i-1} - IMF_i$$

4. Repeat steps 2 with $i = i + 1$ until the number of extreme in r_i is less than 2.

2.1 Image extrema extraction

The first step of the sifting process in the BEMD is to locate the local extrema points (maxima and minima) of the image intensity. The simple way is to use the pixel neighbouring information in the image; such that a point is maxima (respectively minima) if its value is strictly higher (respectively strictly lower) than all its 8-connected closer neighbours.

2.2 Surface interpolation

The interpolation is considered as a delicate stage in the 2D-sifting process it has a remarkable influence on the results of the decomposition. Several techniques have been proposed using, for instance, radial basis functions such as thin-plate splines [26, 27, 22, 28], smoothing spline technique [29]. BEMD, however, requires very high computational cost [22].

2.3 Stopping criterion for the sifting process

The sifting process in the BEMD decomposition consist on decomposing an input signal into set of functions defined by the signal itself, these functions are called BIMFs. A BIMF is characterized by some specific properties.

Each BIMF is expected to have the following properties:

- The number of zero crossings and the number of extrema points is equal or differs by only one.
- The envelopes defined by the local maxima and minima, respectively, are locally symmetric around the envelope mean.

The sifting process stops when the resulting image satisfied the characteristics of a BIMF as it is described above. In other words, it stops when the

envelope mean signal is close enough to zero. After a BIMF is found, we define the residue as the result of subtracting this BIMF from the input image and then we iterate on the residue. The BEMD is completed when the residue, ideally, does not contain any extrema points. This is if we suppose that the sifting process will converge, things that never have been rigorously demonstrated. Then, we should to determine a criterion to stop sifting process; this can be accomplished by limiting the size of the SD which is computed from the two consecutive sifting results. In practice, we have used SD between 0.02 and 0.3 and this stop criterion gives satisfying results.

2.4 Stopping criterion for the decomposition

Generally, the decomposition stops when the number of extrema is less than 2. This means that there are no more oscillations to extract. In some cases we can have a high number of IMFs without meeting this condition, so we should set a maximal number of IMFs to extract. We can stop the decomposition depending on the need; for example, in image denoising we will need only the first IMF.

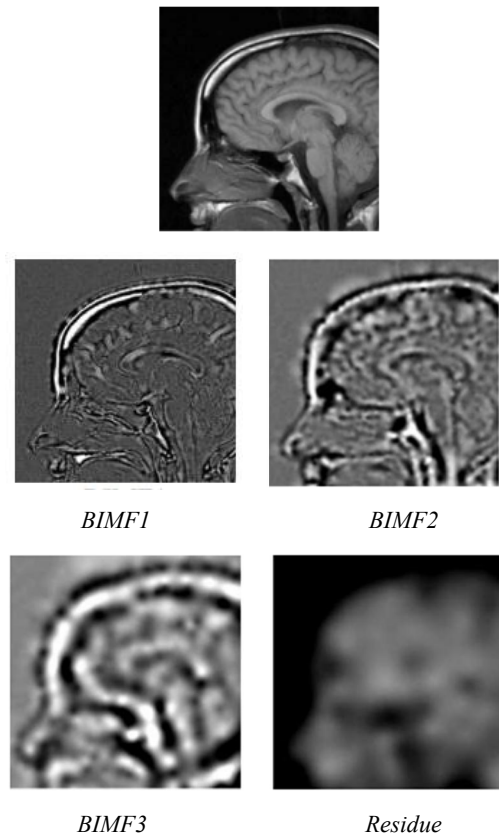


Fig. 1. Decomposition of a medical image using BEMD

3 FAST AND ADAPTIVE BEMD (FABEMD)

The so called FABEMD, proposed by sharif. M et al [30], is a new version of the bidimensional empirical mode decomposition. It is simple, effective, fast and adaptive.

FABEMD decomposition (Fast and Adaptive BEMD) has the same steps as BEMD except that the building envelope average is different from that of the BEMD.

Algorithm

FABEMD differs from the original algorithm BEMD, mainly in the evaluation process of the upper and lower envelopes and in limiting the number of iterations for each BIMF. This change makes the BEMD faster. This is due to the fact that the interpolation step is replaced by spatial processing followed by a smoothing operation. The treatment uses two operators:

- 1) a filter Max to estimate the envelope Max
- 2) a filter Min to estimate the envelope Min

The size of the filter is determined from the extrema matrix Max and Min.

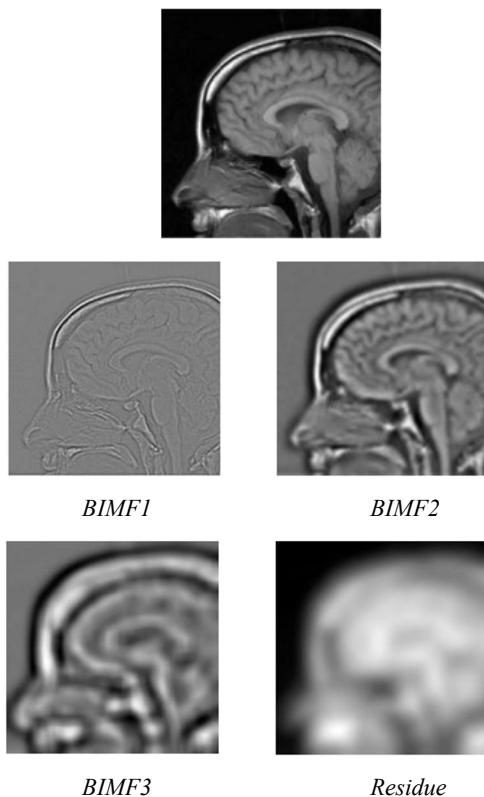


Fig. 2. Decomposition of a medical image using FABEMD

The BIMFs obtained by FABEMD are easier to interpret. On the other hand, contours at different scales are visible on BIMFs obtained by FABEMD. In [30], a study comparing BEMD and FABEMD was presented in detail. It showed that the FABEMD provides a more accurate evaluation of the BIMFs than the BEMD.

4 THREE-DIMENSIONAL RECONSTRUCTION FROM SERIAL SECTIONS

Some technologies are only able to obtain that the surface of the object to be reconstructed as the stereo vision method and the method of the characteristic points. So if you want to explore more than the surface of the object, it is necessary to make sections in the object to be reconstructed. This is the method that is commonly used in medicine and biology. The reconstruction methods depend on the process for obtaining the slices.

The slices can be real or virtual:

- The real slices are obtained by cutting the object physically; this is the case in cytology where cells are sectioned by ultramicrotomy.
- The virtual slices are obtained by using physical properties, acoustic or magnetic of various materials (tissue, bone). This is the case with the Computed tomography (CT), ultrasound, MAGNETIC RESONANCE IMAGING, electron and confocal microscopy.

If the slices are parallel, we say that they are serial sections. And if they are radial slices, we say that they are concentric sections. The real sections are those representing the intersection of the cutting plane and the object. The sections can be projections; in this case it is an accumulation of data taken on lines perpendicular to the section plane (measurement of the intensity resulting from crossing a tissue by an X-ray, for example). It was those kinds of sections we found in Nuclear Magnetic Resonance, Radiography and Computed tomography. The reconstruction used in this case is described by R.Gordon and G.T.Herman [31].

In the case of the surface reconstruction, the focus is only on the surface, and in case of the volume reconstruction, it is the object as a whole is interesting. In some cases only one visualization is used; contrariwise, in other cases an analysis and description of the object are needed to well understand the three-dimensional structure of the object. The type of representation depends on the

use of the 3D object. If the user wants a simple visualization, the surface is sufficient; this is what usually occurs in CAD applications. If the object must constitute a data of a description process, modeling or analysis of 3D objects, it will need whole object. In the general case, the aim is much more than the description of three-dimensional structures encountered as the visual rendering.

Cross sections are increasingly used in many fields to represent 3D objects particularly in medical imaging. But, 3D sampled images do not reflect the real three-dimensional aspect of the object; they simply give a limited and partial view.

The system we propose consists mainly of six steps: acquisition, preprocessing, registration, segmentation, model generation and finally visualization. Second and third stages is somehow preparatory steps for the overall reconstruction process. That is why we have grouped them together to a single step.

4.1 Acquisition step

The information captured by the physical device (a CT scan, MRI or US) is a measure of some physical properties of the body. The result of this step is a sequence of 2D images, usually grayscale, forming the cuts.

4.2 Preprocessing and registration step

On acquisition, external conditions can intervene to affect the quality of the acquired image. The lighting conditions, the level of parasitic signals, nature of the atmosphere (dust, humidity ...), the sampling resolution of the scanner, camera calibration ... All these phenomena add other information called noise. Then, as first phase, we should remove the noise without affecting the useful information. After that, we proceed to improve the quality of the image to facilitate the work of later stages. For this, many studies in the literature offer an extensive range of preprocessing techniques.

In the second phase, the registration of sections takes place. Its role is to realign the cuts in order to get a shape similar to the original subject. In fact, this is necessary where the conditions for obtaining the sequence differ from one section to another, allowing some sections to be rotated or to submit on any deformation. In the case where the sequence consists of sections MRI, CT or US they are aligned, and therefore this step is omitted.

4.3 Segmentation Step

Segmentation is a process to decompose the images sequence into a set of homogeneous regions. Its role in the reconstruction process is to locate the volume of interest (VOI) within the set of sections. Otherwise, the set of pixels representing the same tissue type in a section will be grouped to form a single region, which offers major interest to the practitioner.

A second task assigned to this step is the identification or labeling of the various segmented VOI. Indeed, the segmented regions belonging to the same type of tissue should then be classified according to their anatomical natures. For example, isolating the left ventricle of on the right, or the veins of different arteries. The result is a sequence of binary images where the binary value of each pixel indicates whether it belongs to the VOI. The binary nature of the images greatly reduces the amount of data to be processed.

Another task assigned to this step is to extract, from the volume of interest obtained, all the contours that delimit it, along the sequence of binary images. The final result of this step is a sequence of closed contours plans.

4.4 Modeling Step

This step is the core of the reconstruction process since it builds three-dimensional information. The goal of reconstruction is to provide a geometric description of the digitized object, based mainly on the calculation of a model by volume or by surface which will be an approximation of the set of data. This operation is decomposed into two steps [32]:

- Global connection
- Local connection

The final result of this step is a 3D model, consisting of a mesh, approximating the initial object.

4.5 Visualization step

This is the final step. Visualization is the projection process the 3D model obtained on a 2D plane consisting of the screen for example. This projection should provide the maximum possible information contained in the model, and should also enable an exploration or navigation of the information density presented by this model. In addition, it should allow for intuitive and flexible interaction for user-machine.

In this work, we focused on the third step (segmentation) and the fourth stage (the generation of the 3D model).

The process decomposition approach with BEMD is illustrated in figure 4.

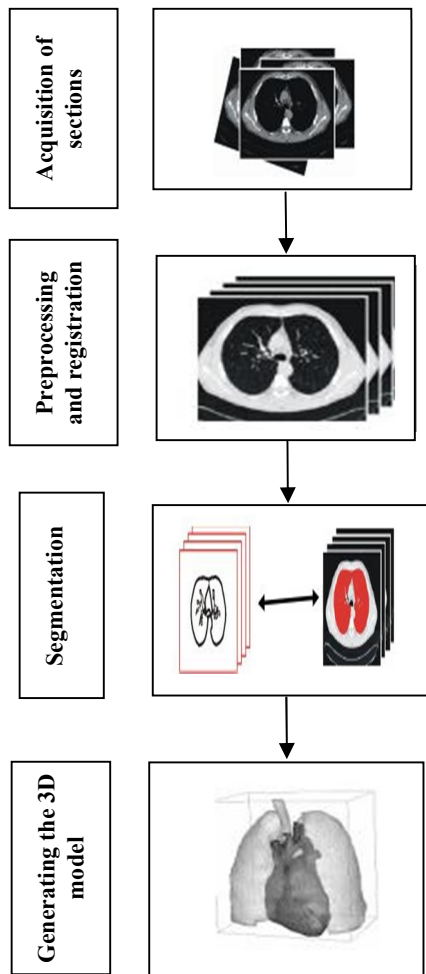


Fig. 3. Principle of the proposed three-dimensional reconstruction system

5 BEMD APPROACH FOR MEDICAL IMAGES

Our approach is based on the application of the decomposition FABEMD for each 2D image in a series of sections. We obtain a set of IMFs and a residue for each image. With the 3D reconstruction of each series of IMFs, we obtain the result image (3D IMF).

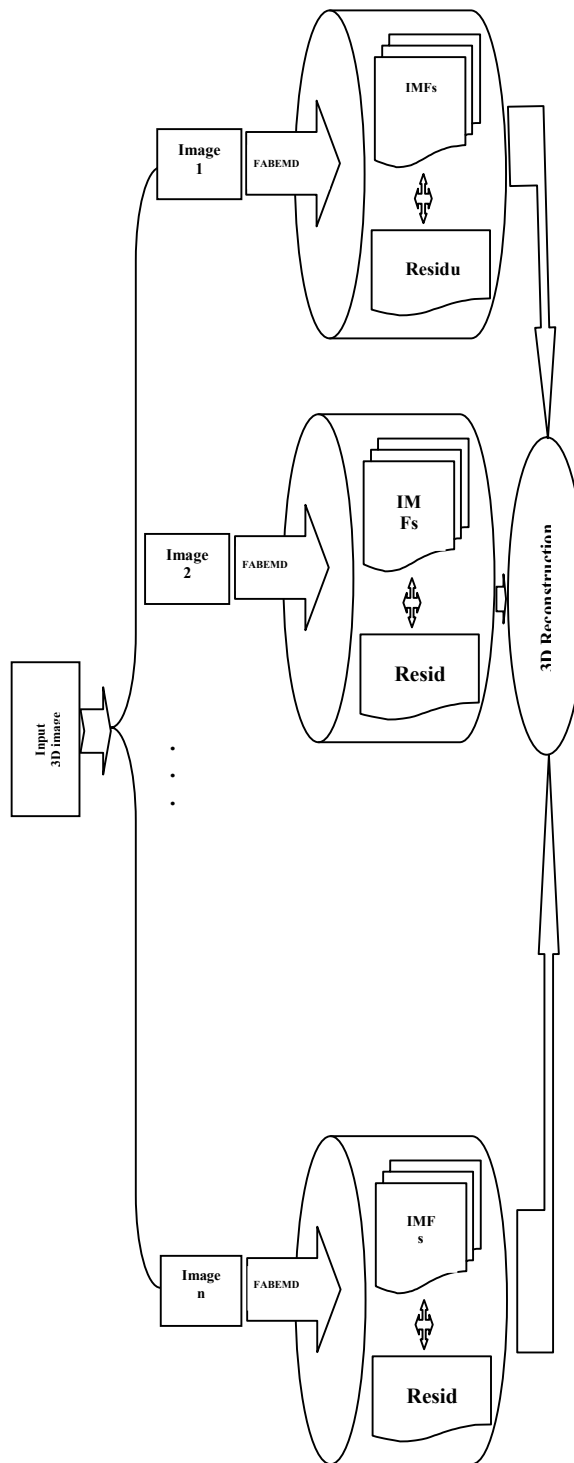


Fig. 4. The BEMD approach for 3D Medical Image

6 EXPERIMENTATION AND RESULTS

In this section we use a series of 55 CT image (Fig. 5) of a pelvis (Fig. 6).

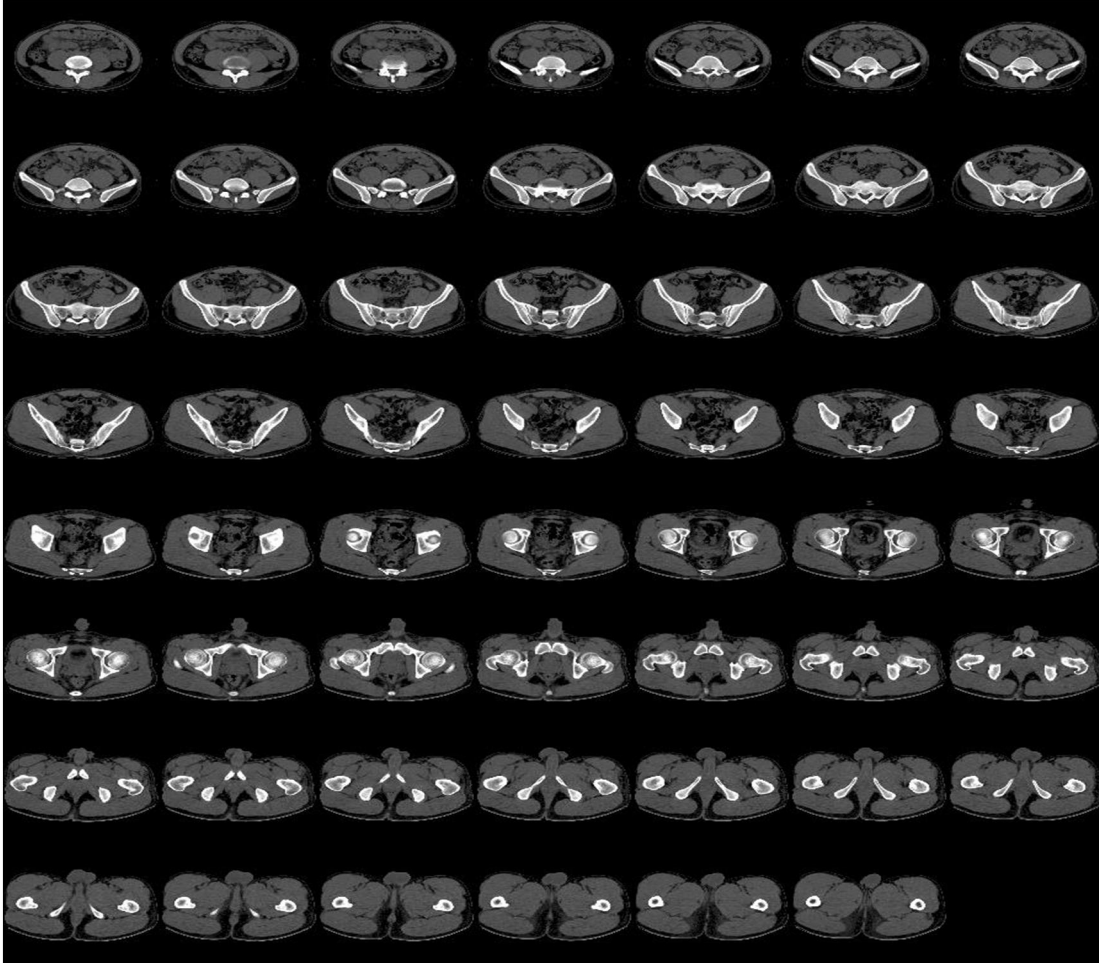


Fig. 5. Series of 55 CT image ordered from left to right and from top to bottom

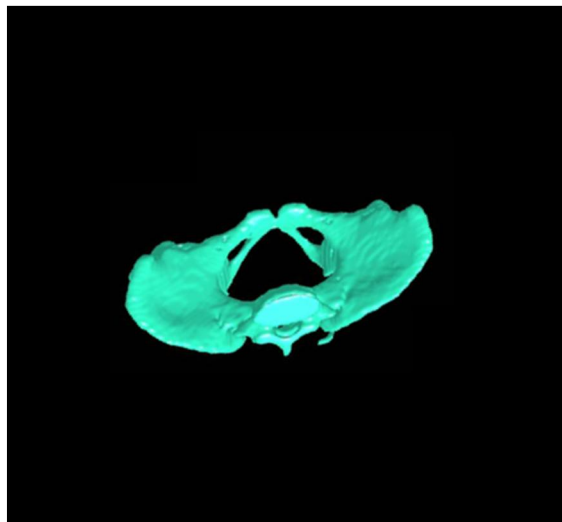
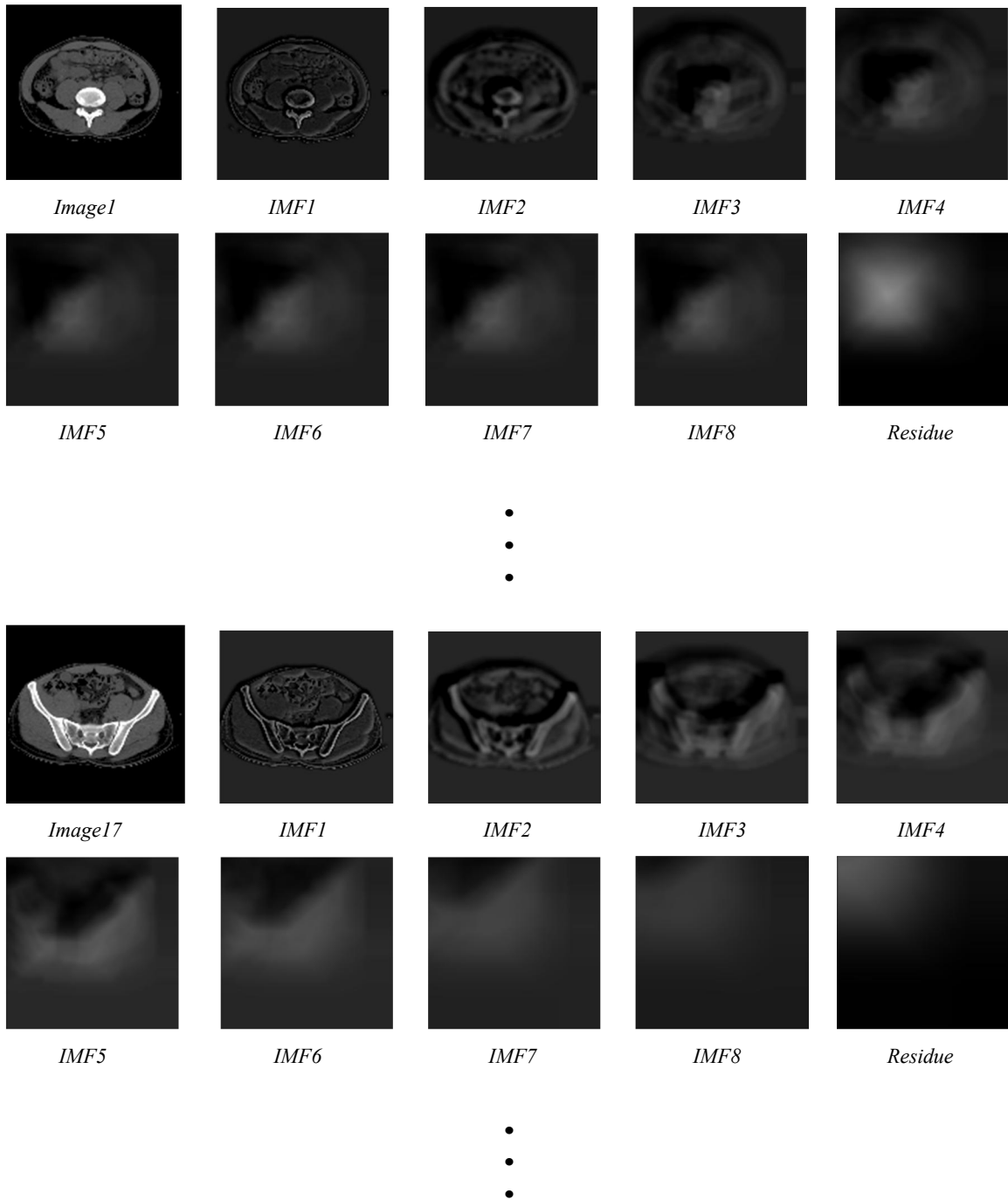


Fig. 6. 3D image of the pelvis

Each image of the previous series is subject to the decomposition FABEMD (Fig. 7).



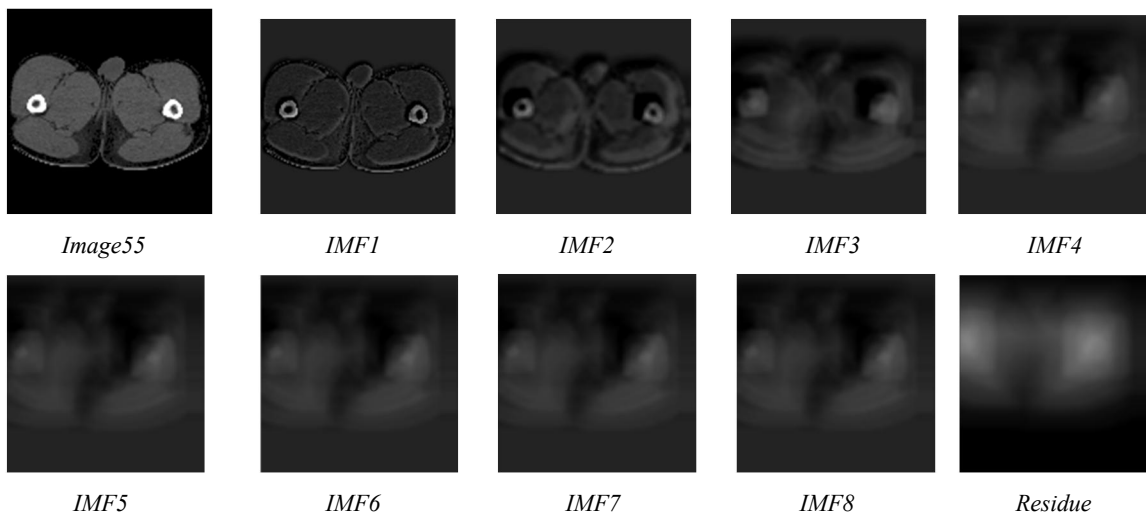
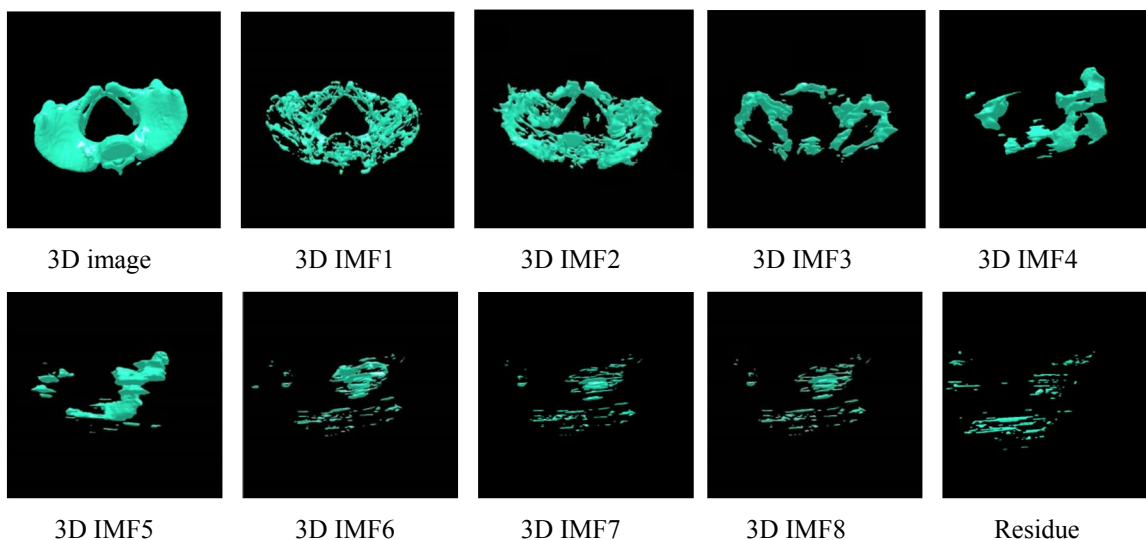


Fig. 7. The result of the decomposition with BEMD for each image in the series of sections

In general, two images do not have the same number of IMFs. If it is the case and in order to construct the 3D IMFs, we duplicate the final IMF of images that have a depth of decomposition inferior than others. For example, in figure 7, image 1 has in fact four IMFs, whereas the image 17 has 8

IMFs which correspond to the maximum depth between the ones of all images of the series. Therefore, to ensure the 3D reconstruction of IMFs we place $IMF8 = IMF7 = IMF6 = IMF5 = IMF4$ and so for all the images that have a depth inferior to 8.



Images in the figure 8 shows the results obtained after the 3D reconstruction of each series of IMFs and the series of the residues.

7 CONCLUSION

In this work, we have presented a technique for implementing the BEMD for medical images

decomposition. BEMD decomposition which has been proven in the case of the 1D signal analysis and has proven a powerful tool for analyzing and interpreting images, its application extend from watermarking, indexing to the image compressing.

The aim of the work was to decompose 3D medical images into 3D IMFs. The medical image can be characterized by global information extracted from the 3D IMFs. We focused on the

problem of 3D reconstruction of 2D images. Three-dimensional reconstruction of objects from serial sections allows for a shift from model previously scanned to a 3D mathematical model reflecting, at the maximum possible, the main properties of the object. This was primarily motivated by the incapacity of 2D imaging to provide a sufficient understanding of both the complexity of the studied objects and the necessity of having a 3D computer representation of many real objects. Problem, widely reported in military applications, industrial, scientific and especially medical, known as 3D reconstruction of serial sections.

As a perspective, we will deal with this problem in its 3D form.

8 REFERENCES

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